17th Annual Workshop on Topology and Dynamical Systems
Nipissing University, May 16-20, 2022
http://topology.nipissingu.ca/workshop2022/

## Complexity of $\eta$ -od-like continua

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Abstract: W. Lewis asked in Indecomposable Continua. Open problems in topology II, whether there exists, for every  $\eta \geq 2$ , an atriodic simple  $(\eta + 1)$ -od-like continuum which is not simple  $\eta$ -od-like and, if such continuum exists, whether it has a variety of properties such as being planar or being an arc-continuum, among others. Some partial results have been obtained by W.T. Ingram, P. Minc, C.T. Kennaugh and L. Hoehn. In each case, the most substantial challenge is in proving that a continuum is not T-like, for a given tree T. We present the notion of a combinatorial  $\eta$ -od cover of a graph, a tool which may enable one to prove that certain examples of continua are not  $\eta$ -od-like. Also, we suggest the construction of an atriodic simple  $(\eta + 1)$ -od-like continuum which is not simple  $\eta$ -od-like and has properties such as being planar, being an arc-continuum, and span zero (This is a work in progress).