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ON LOCAL COMPACTNESS OF SPACES OF CONTINUOUS VALUATIONS

JEAN GOUBAULT-LARRECQ

ABSTRACT. We show that the spaces of continuous valuations, resp. subprobability valuations on a locally compact space is locally compact; similarly with probability valuations on locally compact, compact spaces. Continuous valuations are close cousins of measures. No separation property is assumed.

1. INTRODUCTION

A continuous valuation on a topological space X is a close cousin of a Borel measure. Continuous valuations on X form a space $\mathbf{V}X$, with a topology known as the weak topology, and similarly for the subspaces $\mathbf{V}_{\leq 1}X$ of subprobability valuations and \mathbf{V}_1X of probability valuations. We will define these notions more precisely below. It is known that $\mathbf{V}_{\leq 1}$ preserves various properties: stable compactness [2, Theorem 39], being a continuous dcpo [16, Theorem 5.2], being a quasi-continuous dcpo [14, Theorem 5.1], for example. Some of these preservation theorems extend over to \mathbf{V}_1 or to \mathbf{V} , but a conspicuously absent property in the list is local compactness. This is what we address in this paper.

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